Neural Parts: Learning Expressive 3D Shape Abstractions with Invertible Neural Networks

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 $https://paschalidoud.github.io/neural_parts$



Slides are available at



https://paschalidoud.github.io/talks/neural-parts-presentation.pdf

Can we learn to infer 3D from a 2D image?



Input Image

Neural Network

3D Reconstruction

Taxonomy of 3D Representations

















Reconstruction Accuracy

There exists a **trade-off** between the **number of primitives** and the **reconstruction quality** in primitive-based representations.

Simple parts require a large number of parts for accurate reconstructions.



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Neural Parts yield accurate and semantic reconstructions using an order of magnitude less parts.















Homeomorphism

A homeomorphism is a continuous map between two topological spaces Y and X that preserves all topological properties. In our setup, a homeomorphism $\phi_{\theta} : \mathbb{R}^3 \to \mathbb{R}^3$ is

$$\mathbf{x} = \phi_{m{ heta}}(\mathbf{y})$$
 and $\mathbf{y} = \phi_{m{ heta}}^{-1}(\mathbf{x})$

where **x** and **y** are 3D points in X and Y and $\phi_{\theta} : Y \to X$, $\phi_{\theta}^{-1} : X \to Y$ are continuous bijections.



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For example, geometric object can be seen as topological space, and the **homeomorphism** is a continuous stretching and bending of the object into a new shape.

Parametrizing a Homeomorphism with an INN

A **Real NVP** models a bijective mapping by stacking a sequence of simple bijective transformation functions that scale $(s_{\theta} : \mathbb{R}^2 \to \mathbb{R})$ and translate $(t_{\theta} : \mathbb{R}^2 \to \mathbb{R})$ a set of points from one topological space to another.



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The scale $s_{\theta}(\cdot)$ and the translation $t_{\theta}(\cdot)$ functions can be **implemented with arbitrarily complex networks**.

Input Image



Input Image





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Conditional Homeomorphism

The **original Real NVP cannot be directly applied in our setting** as it does not consider a shape embedding.





$$\begin{aligned} x_o &= x_i \\ y_o &= y_i \\ z_o &= z_i \exp\left(s_{\theta}\left(x_i, y_i\right)\right) + t_{\theta}\left(x_i, y_i\right) \end{aligned}$$

Conditional Homeomorphism

We introduce a conditional coupling layer that implements a bijective mapping conditioned on the per-primitive shape embedding C_m .



What about learning?

Invertible Neural Network



What about learning?



• Implicit Primitive Representation:

$$g^{m}(\mathbf{x}) = \left\|\phi_{\theta}^{-1}(\mathbf{x}; \mathbf{C}_{m})\right\|_{2} - r, \ \forall \ \mathbf{x} \in \mathbb{R}^{3}$$





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What about learning?



• Implicit Representation of predicted shape:

$$G(\mathbf{x}) = \min_{m \in 0...M} g^m(\mathbf{x}),$$

• Explicit Representation of predicted shape:

$$\mathcal{X}_{p} = \{\mathbf{x} \mid \mathbf{x} \in \bigcup_{m} \mathcal{X}_{p}^{m} \text{ s.t. } \mathcal{G}(\mathbf{x}) \geq 0\}$$

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Implicit and Explicit Representation of Predicted Shape



Implicit Representation:

$$G(\mathbf{x}) = \min_{m \in 0...M} g^m(\mathbf{x}),$$

Implicit and Explicit Representation of Predicted Shape



Implicit and Explicit Representation of Predicted Shape



Overall Loss:

 $\mathcal{L} = \mathcal{L}_{\textit{rec}}(\mathcal{X}_t, \mathcal{X}_p) + \ \mathcal{L}_{\textit{occ}}(\mathcal{X}_o) + \ \mathcal{L}_{\textit{norm}}(\mathcal{X}_t) + \mathcal{L}_{\textit{overlap}}(\mathcal{X}_o) + \mathcal{L}_{\textit{cover}}(\mathcal{X}_o)$

Composed of:

- $\circ \quad \mathcal{L}_{\textit{rec}}(\mathcal{X}_t, \mathcal{X}_p) : \text{ Reconstruction Loss}$
- $\circ \quad \mathcal{L}_{\textit{occ}}(\mathcal{X}_{\textit{o}}): \text{ Occupancy Loss }$
- $\circ \ \mathcal{L}_{\textit{norm}}(\mathcal{X}_t)$: Normal Consistency Loss
- $\circ \mathcal{L}_{overlap}(\mathcal{X}_o)$: Overlapping Loss
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Target and Predicted Shape:

- Target:
 - Surface Samples: $X_t = \{\{\mathbf{x}_i, \mathbf{n}_i\}\}_{i=1}^N$

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 - Surface Samples: $\mathcal{X}_t = \{\{\mathbf{x}_i, \mathbf{n}_i\}\}_{i=1}^N$
 - ► Volumetric Samples: $\mathcal{X}_o = \{\{\mathbf{x}_i, o_i\}\}_{i=1}^V$

Overall Loss:

 $\mathcal{L} = \mathcal{L}_{\textit{rec}}(\mathcal{X}_t, \frac{\mathcal{X}_p}{\rho}) + \mathcal{L}_{\textit{occ}}(\mathcal{X}_o) + \mathcal{L}_{\textit{norm}}(\mathcal{X}_t) + \mathcal{L}_{\textit{overlap}}(\mathcal{X}_o) + \mathcal{L}_{\textit{cover}}(\mathcal{X}_o)$

Composed of:

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- **Predicted:** $\mathcal{X}_p = \{\mathbf{x} \mid \mathbf{x} \in \bigcup_m \mathcal{X}_p^m \text{ s.t. } G(\mathbf{x}) \ge 0\}$

Reconstruction Loss



Target Surface Samples: $X_t = \{\{\mathbf{x}_i, \mathbf{n}_i\}\}_{i=1}^N$

Reconstruction Loss



Predicted Surface Samples: $\mathcal{X}_p = \{\mathbf{x} \mid \mathbf{x} \in \bigcup_m \mathcal{X}_p^m \text{ s.t. } G(\mathbf{x}) \ge 0\}$

Reconstruction Loss



$$\mathcal{L}_{rec}(\boldsymbol{\mathcal{X}}_{t}, \boldsymbol{\mathcal{X}}_{p}) = \frac{1}{|\boldsymbol{\mathcal{X}}_{t}|} \sum_{\mathbf{x}_{j} \in \boldsymbol{\mathcal{X}}_{p}} \min_{\mathbf{x}_{j} \in \boldsymbol{\mathcal{X}}_{p}} \|\mathbf{x}_{i} - \mathbf{x}_{j}\|_{2}^{2} + \frac{1}{|\boldsymbol{\mathcal{X}}_{p}|} \sum_{\mathbf{x}_{j} \in \boldsymbol{\mathcal{X}}_{p}} \min_{\mathbf{x}_{i} \in \boldsymbol{\mathcal{X}}_{t}} \|\mathbf{x}_{i} - \mathbf{x}_{j}\|_{2}^{2}$$

Occupancy Loss



Target Volumetric Samples: $X_o = \{\{\mathbf{x}_i, o_i\}\}_{i=1}^V$

Occupancy Loss



Occupancy Loss



Normal Consistency Loss



Target Surface Samples: $\mathcal{X}_t = \{\{\mathbf{x}_i, \mathbf{n}_i\}\}_{i=1}^N$

Normal Consistency Loss



Predicted Surface Normals: $\frac{\nabla_{\mathbf{x}} G(\mathbf{x})}{\|\nabla_{\mathbf{x}} G(\mathbf{x})\|_2}$

Normal Consistency Loss



$$\mathcal{L}_{\textit{norm}}(\mathcal{X}_t) = \frac{1}{|\mathcal{X}_t|} \sum_{(\mathbf{x}, \mathbf{n}) \in \mathcal{X}_t} \left(1 - \left\langle \frac{\nabla_{\mathbf{x}} \mathcal{G}(\mathbf{x})}{\|\nabla_{\mathbf{x}} \mathcal{G}(\mathbf{x})\|_2}, \mathbf{n} \right\rangle \right)$$



Target Volumetric Samples: $X_o = \{\{\mathbf{x}_i, o_i\}\}_{i=1}^V$





$$\mathcal{L}_{overlap}(\mathcal{X}_{o}) = \frac{1}{|\mathcal{X}_{o}|} \max\left(0, \sum_{m=1}^{M} \sigma\left(\frac{-g^{m}(\mathbf{x})}{\tau}\right) - \lambda\right)$$

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Coverage Loss



Target Volumetric Samples: $X_o = \{\{\mathbf{x}_i, o_i\}\}_{i=1}^V$

Coverage Loss



$$\mathcal{L}_{cover}(\mathcal{X}_{o}) = \sum_{m=1}^{M} \sum_{\mathbf{x} \in \mathcal{N}_{k}^{m}} \max\left(0, g^{m}(\mathbf{x})\right)$$

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• **Reconstruction Loss**: The surface of the target and the predicted shape should match.



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- **Occupancy Loss**: The volume of the target and the predicted shape should match.
- **Overlapping Loss**: Prevent overlapping primitives.



- Reconstruction Loss: The surface of the target and the predicted shape should match.
- Normals Consistency Loss: The normals of the target and the predicted shape should match.
- **Occupancy Loss**: The volume of the target and the predicted shape should match.
- **Overlapping Loss**: Prevent overlapping primitives.
- Coverage Loss: Prevent degenerate primitive arrangements.

Representation Power of Primitive-based Representations



Representation Power of Primitive-based Representations





Single-view 3D Reconstruction on D-FAUST



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Single-view 3D Reconstruction on FreiHAND



Single-view 3D Reconstruction on ShapeNet



Single-view 3D Reconstruction on ShapeNet



Single-view 3D Reconstruction on ShapeNet



Semantic Consistency



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Do we really need an INN?



	$\left \right \operatorname{w/o} \phi_{\pmb{\theta}}^{-1}(\mathbf{x})$	AtlasNet - sphere	Ours
loU	0.639	*	0.673
Chamfer-L ₁	0.119	0.087	0.097

What comes next?



Reconstruction Accuracy



Reconstruction Accuracy

• What makes a good primitive-representation?



Reconstruction Accuracy

- What makes a good primitive-representation?
- We learn primitives by optimizing the geometry? Can't we do better?



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Reconstruction Accuracy

- What makes a good primitive-representation?
- We learn primitives by optimizing the geometry? Can't we do better?
- Do we really learn semantic parts?
- Why do we need primitive-based representations?

Learning semantic parts without part-level supervision



Decomposition, 2015

Learning parts through skeletonization

Learning semantic parts without part-level supervision



Learning parts

through skeletonization







Image Source: Unsupervised Discovery of Parts, Structure and Dynamics, 2019

Learning parts from other cues (e.g. motion)

Learning semantic parts without part-level supervision



(a) Curve skeletons derived from our decomposition (GCs are in different colors).



(b) Curve skeletons extracted by ROSA [Tagliasacchi et al. 2009]



(c) Mean curvature skeletons [Tagliasacchi et al. 2012]



(d) Curve skeletons and segmentations obtained by [Au et al. 2008]



(e) Curve skeletons and segmentations obtained by Reniers et al. [2008]

Image Source: Generalized Cylinder Decomposition, 2015

Learning parts through skeletonization



Figure 13: Results of segmenting parts (e-g) and learning hierarchical structure (h) on human motions



Image Source: Unsupervised Discovery of Parts, Structure and Dynamics, 2019

Learning parts from other cues (e.g. motion)



Image Source: Functionality Representations and Applications for Shape Analysis, 2018



Image Source: Relationship Templates for Creating Scene Variations, 2016

The Proposed Where2Act Task



Image Source: Where2Act: From Pixels to Actions for Articulated 3D Objects, 2021

Learning functional parts

Generative model of parts for content creation



Image Source: Google Chimera

Generative model of parts for content creation



Image Source: Attriblt: Content Creation with Semantic Attributes, 2013

Reconstruction by combining parts



Image Source: ShapeAssembly: Learning to Generate Programs for 3D Shape Structure Synthesis, 2020



Image Source:Functional Map Networks for Analyzing and Exploring Large Shape Collections, 2013

Thank you for your attention!